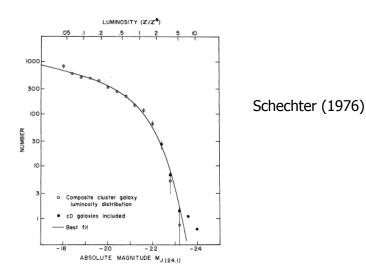
Galaxy Luminosity Function

- Count the number of galaxies as a function of luminosity (or absolute magnitude)
- Useful for:
 - Understanding galaxy formation (distribution by luminosity implies distribution by mass – how many galaxies of a given type and mass were formed)
 - Galaxy evolution models either must reproduce observed LFs (hierarchal formation models) or assume them (and work backwards in time). Can also measure evolution in LFs vs. redshift!
 - Galaxy Properties

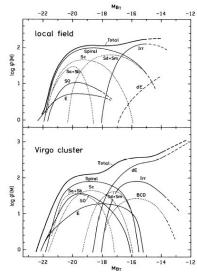
Galaxy Luminosity Function

- Schechter (1976) found that
 - $\Phi(L)dL = \Phi^*(L/L^*)^{\alpha} \exp\{-L/L^*\}d(L/L^*)$
 - $\Phi(L)dL$ = # density of galaxies with luminosities between L and L+dL
 - Where L* is a characteristic luminosity cutoff, α is the power-law slope at the faint end, Φ^* is the normalization (# galaxies/Mpc³)
- · Usually measured in magnitude:
 - $\Phi(M)dM = (0.4ln10)x \Phi^* x 10^{0.4(\alpha+1)(M^*-M)} x exp{-10}^{0.4(M^*-M)}dM$

Schechter Function



Schechter Function by environment

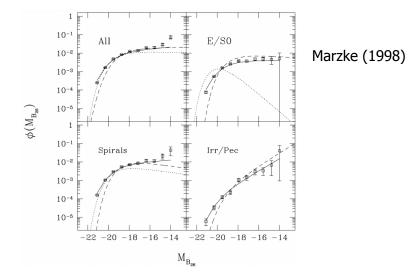


Bingelli (1988)

Field – dominated by Spirals, faint end dIrr

Clusters – many more E/S0 galaxies, faint end dE, more dwarfs than in field

Schechter Function by galaxy type



Approximate Schechter values:

- $M^* \sim -20.5$ (in B), depends on H_0
- L* ~ 2 x 10^{10} L_{\odot} (~Milky Way)
- α ~ -1 to -1.5
- Normalization is uncertain!
- Beware of comparing these numbers, as M* and α are correlated. The Schechter function is just a parametric description.

Integrating the Luminosity Function

- If we integrate the Schechter function, we get the total number of galaxies (per Mpc³), we find:
 - $N = \int_0^\infty \Phi(L) dL = \Phi^* L^* \Gamma(\alpha + 1)$
 - Where Γ is the gamma function, $\Gamma(j+1)=j!$ when j is an integer
 - If α <-1, $\Gamma(\alpha$ +1) is undefined (!), and N is infinite!!
 - We can also integrate to find the total luminosity
 - total lum = $\int_0^{\infty} L\Phi(L)dL = \Phi^* L^* \Gamma(\alpha+2)$, which diverges if $\alpha < -2$
 - so the total amount of light is finite! (Phew!!)

Ellipticals



M89 – E0

Elliptical galaxies:

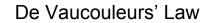
- · Old view (ellipticals are boring, simple systems)
 - Ellipticals contain no gas & dust
 - Ellipticals are composed of old stars
 - Ellipticals formed in a monolithic collapse, which induced violent relaxation of the stars, stars are in an equilibrium state
- New view
 - Some ellipticals have hot x-ray gas, some have dust
 - Ellipticals do rotate (speed varies)
 - Some contain decoupled (counter-rotating) cores
 - Some have weak stellar disks
 - Ellipticals formed by mergers of two spirals, or hierarchical clustering of smaller galaxies

Elliptical galaxies:

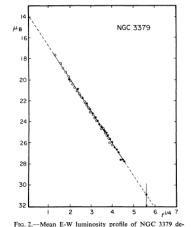
- Separate ellipticals by luminosity:
 - Luminous: L > L*, M_B < -20
 - Midsize: L ~0.1 1 L*, M_B =-18 to –20
 - Dwarfs: L < 0.1 L*, M_B > -18
- Luminous and midsize ellipticals have somewhat different properties, but form a single sequence
- Dwarf E's are significantly different!!

Elliptical galaxies:

- Luminosity profiles (1D):
 - Sersic profile: $I(r) = I(r_e) \exp{-b(r/r_e)^{1/n} 1}$
 - r_e = effective radius which includes half the light (this defines the constant b), and $I(r_e)$ is the surface brightness at r_e
 - Typical elliptical galaxies have n=4, or follow an r^{1/4}-law or "de Vaucouleurs' law" proposed in 1948:
 - $I(r) = I(r_e) \exp\{-7.67 (r/r_e)^{1/4}-1\}$
 - Light in ellipticals more concentrated towards center than for spirals
 - provides good description for surface brightness of mid to bright ellipticals outside the center, but not dE's
 - cD galaxies have an "outer envelope" of extended light
- · Ellipticals show 2D symmetry
 - Some have weak ripples, shells, other fine structure (remnants of mergers?)
 - Also boxy and/or disky isophotes

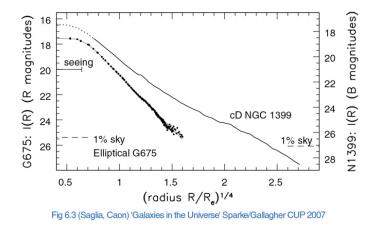


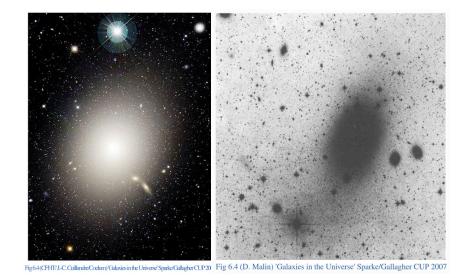
NGC 3379



Fto, 2.—Mean E-W luminosity profile of NGC 3379 derived from McDonald photoelectric data, \bullet , Pe 4 data with 90 cm reflector; \bigcirc , Pe 1 data (M + P) with 2 m reflector. Note close agreement with r^{44} law.

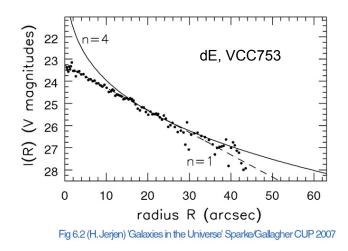
De Vaucouleurs' Law



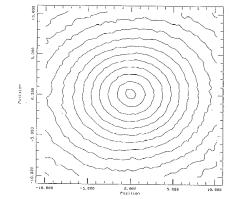


M87 -- see starlight out to 70kpc

Surface Brightness Profiles

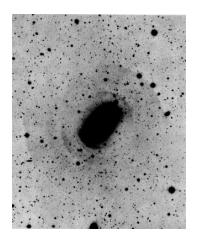


Typical elliptical isophotes



Central regions of the galaxy NGC 4649 out to radii of 10 arcsec. The distance between the isophotes is 0.2 mag. see: P. Surma (1988) *Diploma Thesis*

Shells



NGC 3923

Some ellipticals are not so simple ...



Cen A

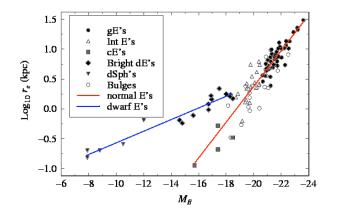
Elliptical galaxies:

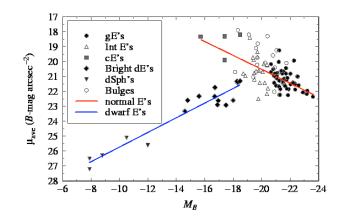
- · In general, ellipticals --
 - Pressure supported (little rotation), stellar motions are (mostly) random
 - No or very little disk component
 - No or very little star formation
 - No or very little cold (e.g., HI) gas, but contain hot, x-ray gas
 - Almost exclusively found in high density environments (clusters)
 - Populate a fundamental plane in luminosity-surface brightness-central velocity dispersion

Elliptical galaxies:

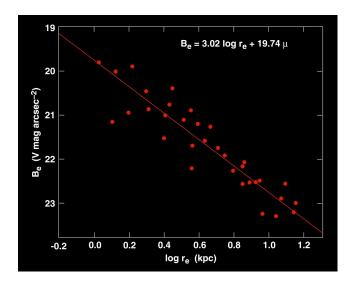
- · There are other correlations
 - Brighter ellipticals are bigger
 - Brighter ellipticals have lower average surface brightness
 - Can put the above two together to form the Kormendy relation larger galaxies have lower surface brightnesses -- $\mu_{B,e}$ = 3.02 log r_e + 19.74
 - Brighter ellipticals have lower central surface brightness
 - Brighter ellipticals have larger core radii -- the core radius is the radius where the SB drops to ½ that of the central SB, I(r=0)

Effective radius vs Absolute magnitude

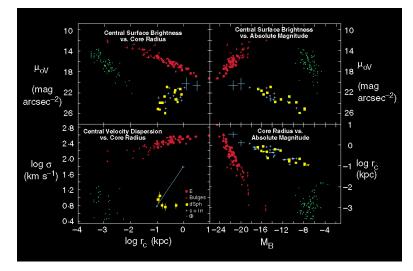




Kormendy relation (1977)

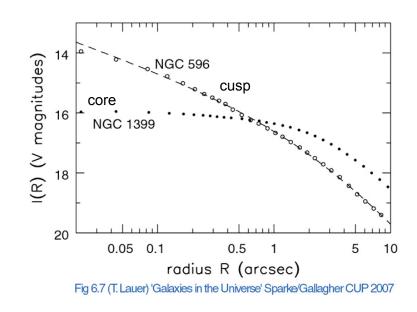


Central surface brightness & core radius relations (Kormendy)

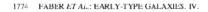


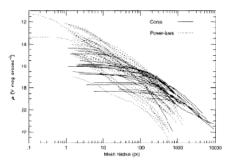
Elliptical galaxies:

- With HST, we can study the nuclei of elliptical galaxies
 - Luminous ellipticals show central cores
 - Mid-sized ellipticals show central cusps, light continues to rise in SB towards center (power-law)

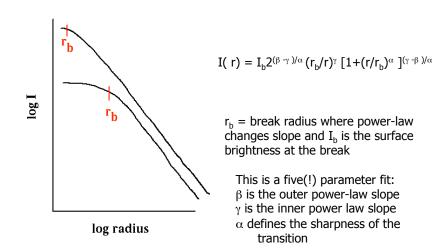


Nuclei of Elliptical Galaxies, Faber et al. 1997



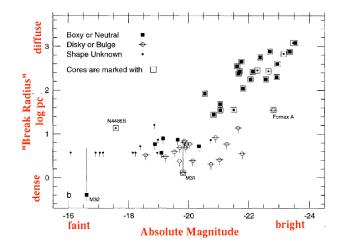


F.a. 1. V-band surface-brightness profiles of 55 ellipticsIs and bulges from kST. All were observed in the WFPC1 Planetary Camera through filter F555W and were deconvolved using the Lucy-Richardson algorithm as described in Faper I. Core galaxies (see Sec. 2) are plotted as solid lines, and power-law galaxies are plotted is dashed lines. "Mean radus" is the geometric mean of the semirajor and seminumor axes of the isophotal ellipse.



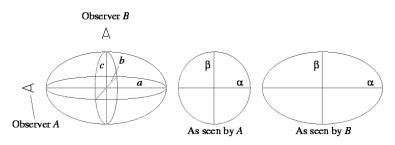
Definition of Break radius

Break radius vs. Absolute magnitude



Shape of Ellipticals:

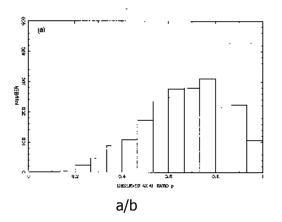
- Ellipticals are defined by En, where n=10ε, and ε=1-b/a is the ellipticity.
- Note this is not intrinsic, it is observer dependent!



Shape of Ellipticals:

- 3-D shapes are ellipticals predominantly:
 - Oblate: A=B>C (a flying saucer)
 - Prolate: A>B=C (a cigar)
 - Triaxial A>B>C (a football)
 - Note A,B,C are intrinsic axis radii
- · Want to derive intrinsic axial ratios from observed
 - Can deproject and average over all possible observing angles to do this
 - Find that galaxies are mildly triaxial:
 - A:B:C ~ 1:0.95:0.65 (with some dispersion ~0.2)
 - Triaxiality is also supported by observations of isophotal twists in some galaxies (would not see these if oblate or prolate)

Observed axial ratio distribution:



Twisty isophotes:

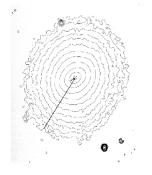
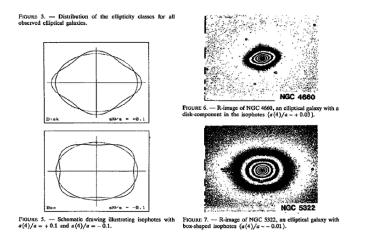


Fig. 4.— Loophotes of the elliptical galaxy NGC 5831 (classified as E3). Notice the isophotal twists from 4 arcseconds to 40 arcseconds (their major-area are indicated in the plot).

NGC 5831

Disky and boxy elliptical isophotes



Examples for boxy and disky isophotes from Bender et al. (1988)

Shape of Ellipticals – disky/boxy

- Galaxies do not have perfect elliptical isophotes typical deviations of a few %
- · Deviations from ellipses can be classified as disky or boxy
- Measure difference between observed isophote and fitted ellipse as:
 - $-\Delta r(t) \approx \sum_{k \ge 3} a_k \cos(kt) + b_k \cos(kt)$
 - t = angle around ellipse, $\Delta r(t)$ is distance between fitted ellipse and observed isophote
 - $a^{}_{3}\,\text{and}\,b^{}_{3}\,\text{describe "egg-shaped" ellipses, generally small, b4 is also usually small$
 - $-a_4 > 0$, isophote is disky (pushed out)
 - $-a_4 < 0$ isophote is boxy (peanut shaped)

Shape of Ellipticals – disky/boxy

- Disky/boxy correlates with other galaxy parameters:
 - Boxy galaxies more likely to show isophotal twists (and hence be triaxial)
 - Boxy galaxies tend to be more luminous
 - Boxy galaxies have strong radio and x-ray emission
 - Boxy galaxies are slow rotators
 - In contrast disky galaxies are midsized ellipticals, oblate, faster rotators, less luminous x-ray gas